

EXAMPLE 2

on p. 516
for Exs. 12–23

SOLVING EXPONENTIAL EQUATIONS Solve the equation.

12. $8^x = 20$

13. $e^{-x} = 5$

14. $7^{3x} = 18$

15. $11^{5x} = 33$

16. $7^{6x} = 12$

17. $4e^{-2x} = 17$

18. $10^{3x} + 4 = 9$

19. $-3e^{2x} + 16 = 5$

20. $0.5^x - 0.25 = 4$

21. $\frac{1}{3}(6)^{-4x} + 1 = 6$

22. $2^{0.1x} - 5 = 7$

23. $\frac{3}{4}e^{2x} + \frac{7}{2} = 4$

EXAMPLE 4

on p. 517
for Exs. 24–31

SOLVING LOGARITHMIC EQUATIONS Solve the equation. Check for extraneous solutions.

24. $\log_5(5x + 9) = \log_5 6x$

25. $\ln(4x - 7) = \ln(x + 11)$

26. $\ln(x + 19) = \ln(7x - 8)$

27. $\log_5(2x - 7) = \log_5(3x - 9)$

28. $\log(12x - 11) = \log(3x + 13)$

29. $\log_3(18x + 7) = \log_3(3x + 38)$

30. $\log_6(3x - 10) = \log_6(14 - 5x)$

31. $\log_8(5 - 12x) = \log_8(6x - 1)$

**EXAMPLES
5 and 6**

on pp. 517–518
for Exs. 32–44

EXPONENTIATING TO SOLVE EQUATIONS Solve the equation. Check for extraneous solutions.

32. $\log_4 x = -1$

33. $5 \ln x = 35$

34. $\frac{1}{3} \log_5 12x = 2$

35. $5.2 \log_4 2x = 16$

36. $\log_2(x - 4) = 6$

37. $\log_2 x + \log_2(x - 2) = 3$

38. $\log_4(-x) + \log_4(x + 10) = 2$

39. $\ln(x + 3) + \ln x = 1$

40. $4 \ln(-x) + 3 = 21$

41. $\log_5(x + 4) + \log_5(x + 1) = 2$

42. $\log_6 3x + \log_6(x - 1) = 3$

43. $\log_3(x - 9) + \log_3(x - 3) = 2$

44. **THINKING CRITICALLY** What is the solution of $3 \log_8(2x + 7) + 8 = 10$?

(A) -1.5

(B) -1.179

(C) 4

(D) 4.642

ERROR ANALYSIS Describe and correct the error in solving the equation.

45.

$3^{x+1} = 6^x$

$\log_3 3^{x+1} = \log_3 6^x$

$x + 1 = x \log_3 6$

$x + 1 = 2x$

$1 = x$



46.

$\log_3 10x = 5$

$e^{\log_3 10x} = e^5$

$10x = e^5$

$x = \frac{e^5}{10}$



47. **OPENING PROBLEM SOLVING** Give an example of an exponential equation whose only solution is 4 and an example of a logarithmic equation whose only solution is -3.

CHALLENGE Solve the equation.

48. $3^{x+4} = 6^{2x-5}$

49. $10^{3x-8} = 2^{5-x}$

50. $\log_2(x + 1) = \log_8 3x$

51. $\log_3 x = \log_9 6x$

52. $2^{2x} - 12 \cdot 2^x + 32 = 0$

53. $5^{2x} + 20 \cdot 5^x - 125 = 0$