CHAPTER SUMMARY

BIG IDEAS

For Your Notebook



Graphing Rational Functions

Use the following steps to graph $f(x) = \frac{p(x)}{q(x)} = \frac{a_m x^m + a_{m-1} x^{m-1} + \dots + a_1 x + a_0}{b_n x^n + b_{n-1} x^{n-1} + \dots + b_1 x + b_0}$

where p(x) and q(x) have no common factors other than ± 1 .

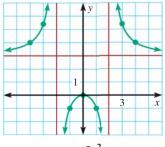
STEP 1 Plot the *x*-intercepts. The *x*-intercepts are the real zeros of
$$p(x)$$
.

STEP 2 Draw the vertical asymptote(s). A vertical asymptote occurs at each real zero of
$$q(x)$$
.

If
$$m < n$$
, $y = 0$ is a horizontal asymptote.

If
$$m = n$$
, $y = \frac{a_m}{b_n}$ is a horizontal asymptote.

If m > n, there is no horizontal asymptote.



$$y = \frac{3x^2}{x^2 - 4}$$

STEP 4 Plot several points on both sides of each vertical asymptote.



Performing Operations with Rational Expressions

Operation	Example
Simplify Divide out common factors from the numerator and denominator.	$\frac{x^2 + 3x}{x^2 + 8x + 15} = \frac{x(x+3)}{(x+5)(x+3)} = \frac{x}{x+5}$
Multiply Multiply numerators and denominators. Then simplify.	$\frac{x}{15} \cdot \frac{3}{x^2 + 7x} = \frac{3x}{15x(x+7)} = \frac{1}{5(x+7)}$
Divide Multiply the first expression by the reciprocal of the second expression. Then simplify.	$\frac{x^2}{3x+1} \div \frac{1}{6x+2} = \frac{x^2}{3x+1} \cdot \frac{2(3x+1)}{1} = 2x^2$
Add or Subtract Write the expressions with like denominators. Then add or subtract the numerators over the common denominator. Lastly, simplify.	$\frac{5}{x} + \frac{x}{x+2} = \frac{5(x+2)}{x(x+2)} + \frac{x^2}{x(x+2)} = \frac{x^2 + 5x + 10}{x(x+2)}$



Solving Rational Equations

Solve
$$\frac{x}{x+1} + \frac{2}{x+4} = 1$$
.

LCD is
$$(x + 1)(x + 4)$$
.

$$x(x + 4) + 2(x + 1) = (x + 1)(x + 4)$$

$$x^2 + 4x + 2x + 2 = x^2 + 5x + 4$$

$$6x + 2 = 5x + 4$$

$$x = 2$$